

Name 2/11/2020 Hour _____ Date _____

Algebra 2: Equation of a Parabola, via “completing the square”

vertex form: $y = \frac{1}{4p} (x - h)^2 + k$
vertical parabola

$x = \frac{1}{4p} (y - k)^2 + h$
horizontal parabola

Warm-up

1.) What is the vertex of $y = 2(x + 1)^2 - 4$

$$V(-1, -4)$$

2.) What is the vertex of $x = \frac{1}{2}(y + 5)^2 + 8$

$$V(8, -5)$$

However, sometimes the equation isn't in this friendly vertex form!

There's another way to write the equation of a Parabola!!!

standard form: $y = ax^2 + bx + c$

Example 1: $x^2 + 12x + 26$ What is the vertex!?!?!? Ugh... just

like what we did with the circle, we have to “complete the square.” Let’s do it!

$$x^2 + 12x + \boxed{36} + 26 - \boxed{-36}$$

↓
Half, Squared

$$(x + 6)^2 - 10 \quad \text{Vertex } (-6, -10)$$

Example 2: $x^2 - 14x + 58$

$$x^2 - 14x + \boxed{49} + 58 - \boxed{-49}$$

$$(x - 7)^2 + 9 \quad \text{Vertex } (7, 9)$$

* Example 3: $2x^2 + 8x + 12$

$$2x^2 + 8x + \boxed{} + 12 - \boxed{}$$

$$2(x^2 + 4x + \boxed{4}) + 12 - \boxed{8}$$

$$2(x + 2)^2 + 4 \quad \text{Vertex: } (-2, 4)$$